

CS 440 Theory of Algorithms

Fundamental Data Structures

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Fundamental Data Structures

- **Linear structures**
 - **Array**
 - **Linked list**
 - **Singly linked list**
 - **Doubly linked list**
 - **Stack**
 - **Queue**
- **Graph**
 - **Adjacency matrix**
 - **Adjacency list**
- **Trees**
 - **Binary trees**
 - **Binary search trees**

Array and Linked List



FIGURE 1.3 Array of n elements

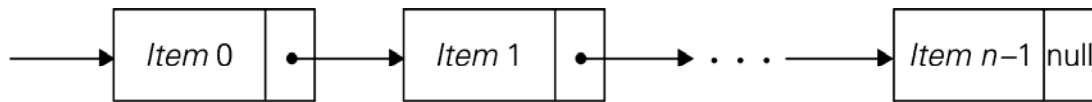


FIGURE 1.4 Singly linked list of n elements

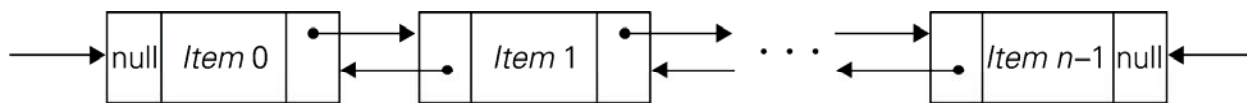


FIGURE 1.5 Doubly linked list of n elements

Graph

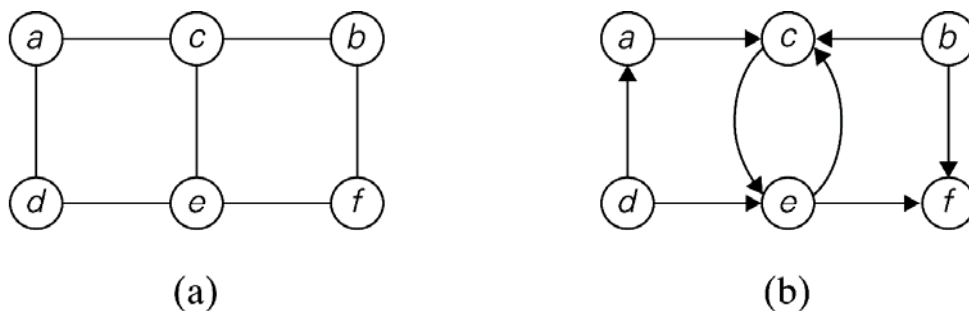
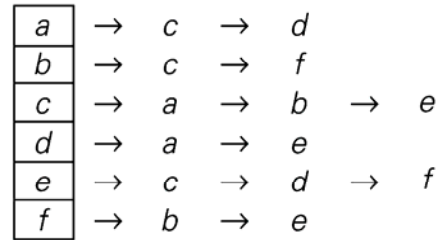


FIGURE 1.6 (a) Undirected graph. (b) Digraph.

Graph Representations

$$\begin{array}{c}
 a \\
 b \\
 c \\
 d \\
 e \\
 f
 \end{array}
 \begin{bmatrix}
 a & b & c & d & e & f \\
 0 & 0 & 1 & 1 & 0 & 0 \\
 0 & 0 & 1 & 0 & 0 & 1 \\
 1 & 1 & 0 & 0 & 1 & 0 \\
 1 & 0 & 0 & 0 & 1 & 0 \\
 0 & 0 & 1 & 1 & 0 & 1 \\
 0 & 1 & 0 & 0 & 1 & 0
 \end{bmatrix}$$

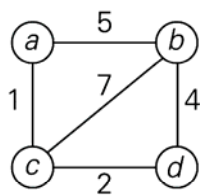
(a)



(b)

FIGURE 1.7 (a) Adjacency matrix and (b) adjacency lists of the graph in Figure 1.6a

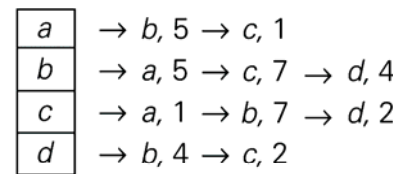
Graph Representations



(a)

$$\begin{array}{c}
 a \\
 b \\
 c \\
 d
 \end{array}
 \begin{bmatrix}
 a & b & c & d \\
 \infty & 5 & 1 & \infty \\
 5 & \infty & 7 & 4 \\
 1 & 7 & \infty & 2 \\
 \infty & 4 & 2 & \infty
 \end{bmatrix}$$

(b)



(c)

FIGURE 1.8 (a) Weighted graph. (b) Its weight matrix. (c) Its adjacency lists.

Graph – Disconnected Graph

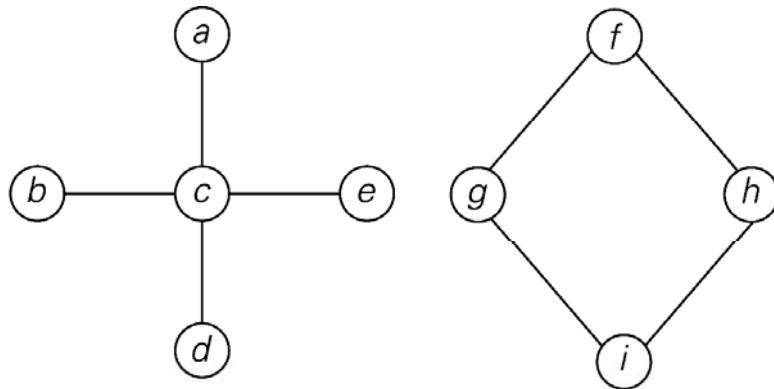


FIGURE 1.9 Graph that is not connected

Tree

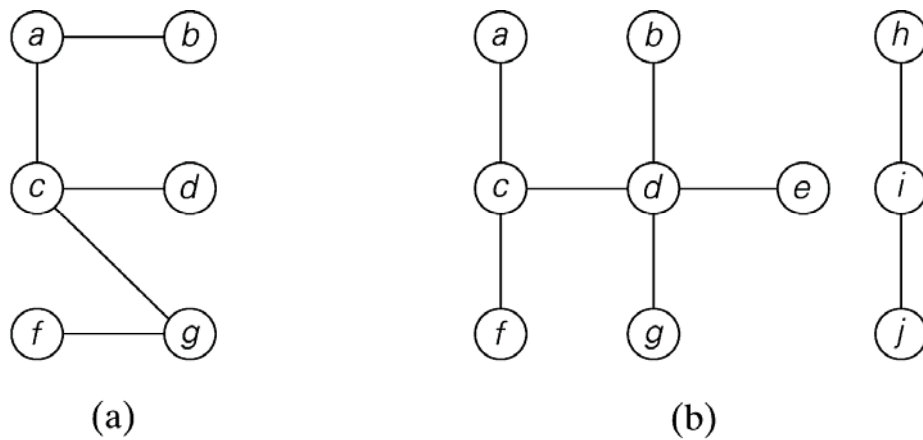


FIGURE 1.10 (a) Tree. (b) Forest.

Rooted Tree

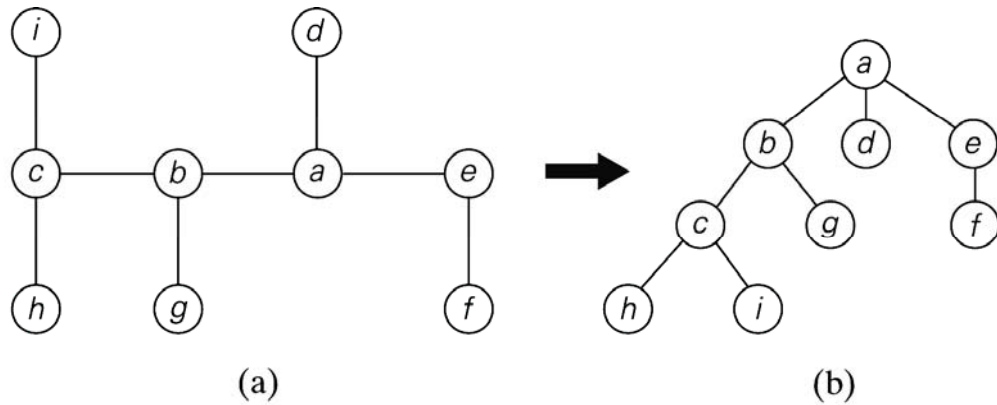


FIGURE 1.11 (a) Free tree. (b) Its transformation into a rooted tree.

Binary Tree and Binary Search Tree

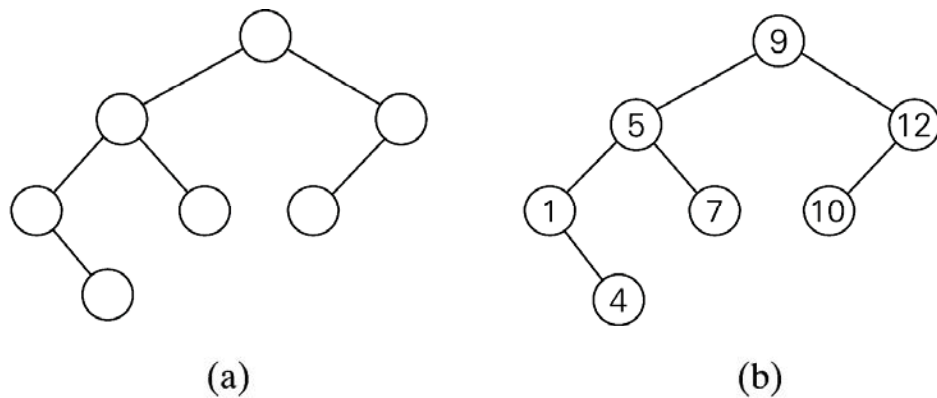


FIGURE 1.12 (a) Binary tree. (b) Binary search tree.

Binary Search Tree

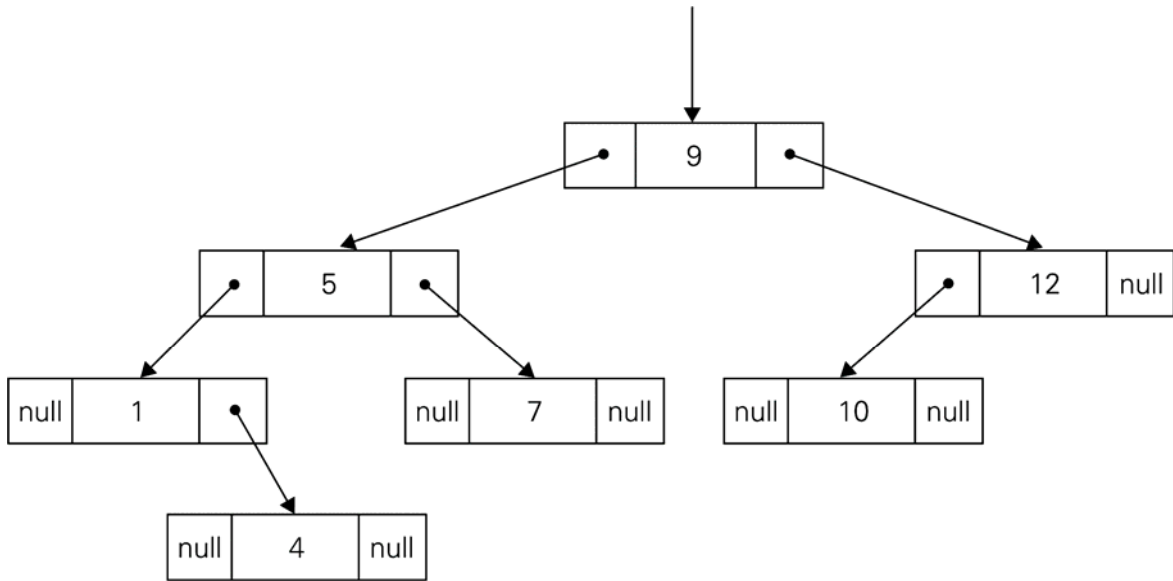


FIGURE 1.13 Standard implementation of the binary search tree in Figure 1.12b

General Tree Representation

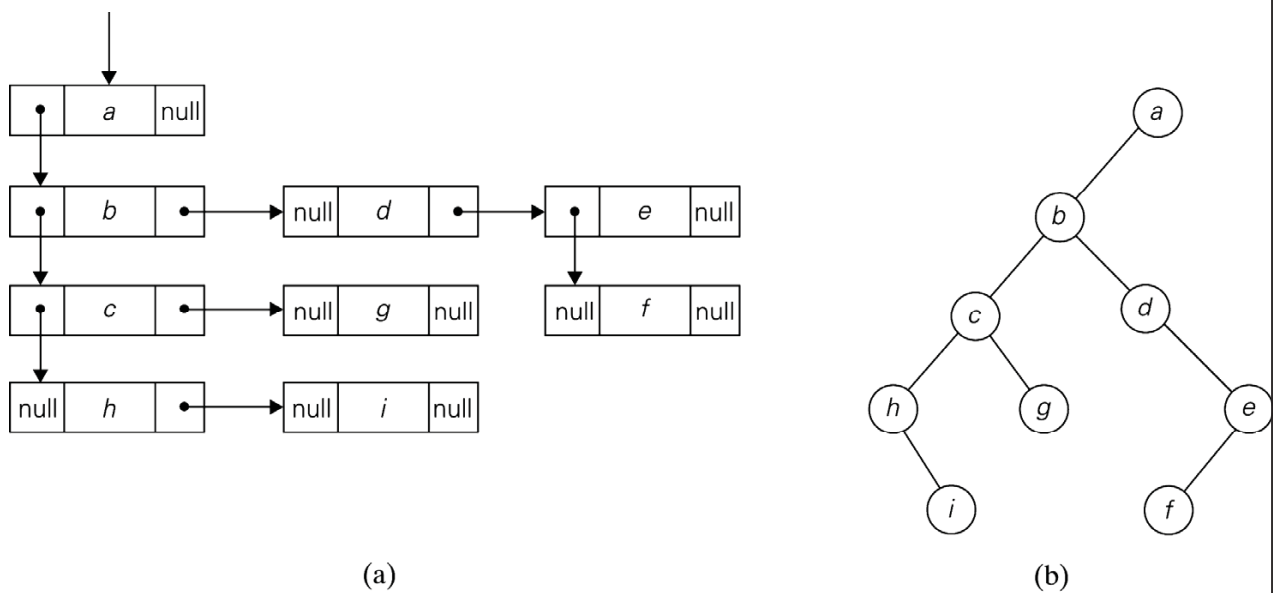


FIGURE 1.14 (a) First child-next sibling representation of the graph in Figure 1.11b. (b) Its binary tree representation.